

### Structural model

#### DESCRIPTION:

#### [LONGITUDINAL]

input = { }

#### PK:

#### EQUATION:

#### DEFINITION:

#### OUTPUT:

output = { }  
table = { }

#### DESCRIPTION: block

Optional text describing the model

#### [LONGITUDINAL] section

Contains the structural model with:

- **input = { } list**  
parameters that are estimated or used as regressor variables.
- **PK: block**  
permits to define PK models using macros, and to link the administration information of the data set with the model.
- **EQUATION: block**  
mathematical equations including ODEs and DDEs.
- **DEFINITION: block**  
used to define a random variable and its probability distribution.
- **OUTPUT: block**  
contains the [LONGITUDINAL] section outputs.
  - **output = { } list**  
identifies the predictions or the modeled outputs that are fitted against the data set observations.
  - **table = { } list**  
parameters or variables outputted in the result folder of Monolix.

### Modeling discrete data with DEFINITION:

#### Time-to-event model

#### DEFINITION:

Event = {type=event, maxEventNumber=1, hazard=h}

- **Event:** name of the random variable, can be replaced by any name. It should be listed in the outputs, to be matched to the observed data.
- **hazard:** hazard function, can be defined via an expression in EQUATION:.
- Indicating the maximum number of events in the **maxEventNumber** argument speeds up calculations.

#### Count model

#### DEFINITION:

CountNumber = {type=count, P(CountNumber=k) = ...}

- **CountNumber:** name of the random variable, can be replaced by any name. It should be listed in the outputs, to be matched to the observed data.
- **k** is a mandatory name for the values. The probability mass function **P(CountNumber=k)** should be defined as a function of **k** and individual parameters.
- It is possible to define directly the log of the probability mass function with:  $\log(P(\text{CountNumber}=k)) = \dots$ .

#### Categorical model

#### DEFINITION:

level = {type = categorical, categories = {0, 1, 2},  
 $\logit(P(\text{level} \leq 0)) = \text{th1}$   
 $\logit(P(\text{level} \leq 1)) = \text{th1} + \text{th2}$ }

- **categories:** list of ordered categories, as increasing successive integers.
- **P(Y=i):** probability of a given category integer *i*, for the observation named *Y*. A transformed probability can be provided instead of a direct one. The transformation can be log, logit, or probit.
- The model is completely defined by the probability mass functions  $P(Y=i)$  for each category, or the cumulative probabilities  $P(Y \leq i)$ .
- When the value of a probability can be deduced from others, its definition can be spared.

### Arguments

#### Compartment characteristics

<b>amount</b>	Variable for drug amount in the compartment
<b>concentration</b>	Variable for drug concentration in the compartment
<b>volume, V</b>	Compartment volume

#### Administration

<b>adm</b>	Administration type to map with ADMINISTRATION ID from dataset, optional: default value is 1
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#### Targets

<b>cmt</b>	Label of compartment (integer)
<b>target</b>	ODE variable

#### Absorption

<b>Tk0</b>	Zero-order duration
<b>ka</b>	First-order rate
<b>p</b>	Fraction of absorbed drug

#### Delays

<b>Tlag</b>	Lag time
<b>Ktr</b>	Transit rate
<b>Mtt</b>	Mean transit time

#### Transfers

<b>kt</b>	Transfer rate from one compartment to another
<b>kij, kji</b>	Transfer rates between compartments <i>i</i> and <i>j</i>
<b>ke0</b>	Transfer rate to an effect compartment

#### Elimination

<b>k</b>	Elimination rate
<b>Cl</b>	Clearance
<b>Vm, Km</b>	Michaelis-Menten elimination

### pkmodel macro

**pkmodel**(V, k/Cl/(Vm, Km),  
Tlag/(Ktr, Mtt), p, Tk0/ka,  
(k12, k21), (k13, k31), ke0)

Defines common PK models with a list of parameters. Single administration type and single elimination only.

#### Administration macros

Administration macros apply the doses from the dataset to the model. Dose types indicated in the column ADMINISTRATION ID are mapped with the argument adm.

#### Targeting a compartment

**absorption**(adm=..., cmt=...,  
Tlag/(Ktr, Mtt), p, Tk0/ka)

For first-order or zero-order absorption arriving in cmt compartment.

**iv**(adm=..., cmt=..., Tlag, p)

For bolus or infusion into cmt.

#### Targeting an ODE variable

**depot**(adm=..., target=...,  
Tlag/(Ktr, Mtt), p, Tk0/ka)

For first-order or zero-order absorption, bolus or infusion. Amount applied to the ODE variable in target.

**reset**(adm=..., target=...)

Resets the target variable to its initial value at the corresponding dosing times in the dataset (dose value not used).

**empty**(adm=..., target=...)

Sets the target variable to 0 at the corresponding dosing times in the dataset (dose value not used).

### Compartment macros

**compartment**(cmt=...,  
amount/concentration=...,  
volume=...)

Defines a compartment that can be used in other macros. Needs to be defined first.

**peripheral**(kij, kji,  
amount/concentration=...,  
volume=...)

Defines a peripheral compartment of label *j* with two transfers of drug amount from and toward the compartment of label *i*.

**effect**(cmt=..., ke0,  
concentration=...)

Defines an effect compartment with a transfer of drug from compartment cmt.

**transfer**(from=i, to=j, kt)

Unidirectional transfer process from compartment *i* to compartment *j*.

### Elimination macro

**elimination**(cmt=...,  
k/Cl/(Vm, Km))

Defines an elimination from compartment cmt.

/: Mutually exclusive  
( ): Mutually dependent  
Mandatory arguments

### Syntax for equations and ODEs

#### Syntax

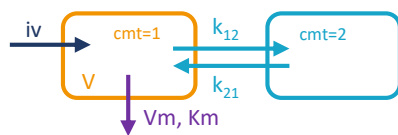
**ddt\_x:** time derivative of variable *x* (*x* can be any name)  
**t\_0:** initial value of time  
**x\_0:** initial value of variable *x*  
**if, elseif, else, end:** conditional statements  
**a\*b, a/b, a^b:** math operators  
**a==b, a<b, a<=b, a>b, a&b, a|b:** logical operators  
**exp, log, log10, sqrt, cos, sin, factln, max, min ...:** math functions

#### Keywords

**t:** time  
**tDose:** time of the last administered dose  
**amtDose:** amount of the last administered dose  
**infDose:** infusion time of the last administered dose  
**delay(x,tau):** delay function for DDEs  
**odeType=stiff:** use a stiff ODE solver (add in EQUATION:)  
Comments begin with ;

# Examples

## Two-compartment model with iv bolus or infusion and Michaelis-Menten elimination



**[LONGITUDINAL]**  
**input** = {V, Vm, Km, k12, k21}  
**EQUATION:**  
 Cc = pkmodel(V, Vm, Km, k12, k21)  
**OUTPUT:**  
**output** = Cc

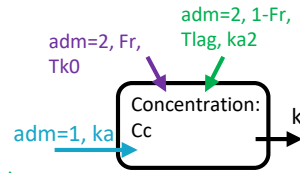
This model is available in the PK models library.

## Two formulations: 1<sup>st</sup> order absorption and mixed 0-order/ 1<sup>st</sup> order absorption

**[LONGITUDINAL]**  
**input** = {V, ka, Tk0, ka2, Fr, k}

**PK:**  
 compartment(cmt=1, volume=V, concentration=Cc)  
 absorption(adm=1, cmt=1, ka)  
 absorption(adm=2, cmt=1, Tk0, p=Fr)  
 absorption(adm=2, cmt=1, Tlag=Tk0, ka=ka2, p=1-Fr)  
 elimination(cmt=1, k)

**OUTPUT:**  
**output** = Cc



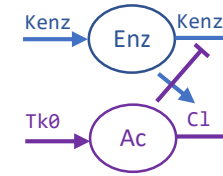
The two formulations should be distinguished in the dataset with the column ADMINISTRATION ID.

## Auto-induction model for time-varying clearance

**[LONGITUDINAL]**  
**input**={Tk0, V, Cl, Kenz, IC50}

**PK:**  
 depot(target=Ac, Tk0)

**EQUATION:**  
 t\_0 = 0  
 Ac\_0 = 0  
 Enz\_0 = 1



**ddt\_Ac** = - Cl/V\*Ac\*Enz  
**ddt\_Enz** = Kenz - Kenz \* (1 - Cc/(Cc+IC50)) \* Enz  
**Cc** = Ac/V

**OUTPUT:**  
**output** = {Cc}

The drug stimulates its own metabolism via induction of the metabolic enzyme expression.

## PK-PD-TTE: joint model for plasma concentration, tumor volume and death

**[LONGITUDINAL]**

**input**={V, Cl, Q, V2, Vm, Km, Mini, kp, kd, R, lambda0, betaM}

**PK:**  
 compartment(cmt=1, amount=Ac, volume=V, concentration=Cc)  
 peripheral(k12=Q/V, k21=Q/V2)  
 elimination(cmt=1, Cl)  
 elimination(cmt=1, Vm, Km)  
 iv(adm=1, cmt=1)

**EQUATION:**  
 odeType= stiff  
 t\_0 = 0  
 M\_0 = Mini  
 ddt\_M = (kp - kd\*Cc\*exp(-R\*t))\*M

**Msat** = min(1000, M)  
**lambda** = lambda0\*exp(betaM\*Msat)

**DEFINITION:**  
 death = {type=event, eventType= exact, maxEventNumber=1, hazard = lambda}

**OUTPUT:**  
**output** = {Cc, M, death}

The statement odeType=stiff permits to use a stiff ODE solver.

## Dose-dependent bioavailability

Using dose-related keywords: amtDose

**[LONGITUDINAL]**  
**input** = {ka, k, V, D50}

**PK:**  
 F = amtDose / (amtDose + D50)  
 Cc = pkmodel(ka, V, k, p=F)

**OUTPUT:**  
**output** = {Cc}

Using a regressor containing the dose information

**[LONGITUDINAL]**  
**input** = {ka, k, V, DoseReg, D50}  
 DoseReg = {use=regressor}

**PK:**  
 F = DoseReg / (DoseReg + D50)  
 Cc = pkmodel(ka, V, k, p=F)

**OUTPUT:**  
**output** = {Cc}

## Count model: zero-inflated Poisson model

**[LONGITUDINAL]**  
**input** = {lambda0, nu, f}

**EQUATION:**  
 lambda = lambda0\*exp(-t/nu)

**DEFINITION:**  
 CountNumber = {type=count, if k==0  
 Pk = exp(-lambda)\*(1-f) + f  
 else  
 Pk = exp(k\*log(lambda) - lambda - factln(k))\*(1-f)  
 end  
 P(CountNumber=k) = Pk}

**OUTPUT:**  
**output** = CountNumber

The output is the number of events (in {0, ..., infinity}) with an inflation of zero counts. Lambda decreases exponentially over time.

## PK-urine: joint model with plasma concentration and amount in urine

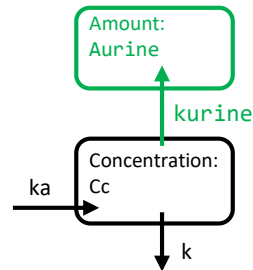
**[LONGITUDINAL]**  
**input** = {ka, Cl, V, p\_urine}

**PK:**  
 depot(adm=1, target=Ac, ka)  
 empty(adm=2, target=Aurine)

**EQUATION:**  
 k\_urine = p\_urine\*Cl/V  
 k\_non\_urine = (1-p\_urine)\*Cl/V

t\_0 = 0  
 Ac\_0 = 0  
 Aurine\_0 = 0  
 ddt\_Ac = - k\_non\_urine\*Ac - k\_urine\*Ac  
 ddt\_Aurine = k\_urine\*Ac  
 Cc = Ac/V  
 thalf = log(2)\*V/Cl

**OUTPUT:**  
**output** = {Cc, Aurine}  
**table** = {thalf}



Times of emptying of urine compartment are encoded in the dataset as pseudo-doses with ADMINISTRATION ID=2. A table of values for the elimination half-life thalf is outputted in the result folder at each observation time.